
Equivalence of big and small steps

Method bodies and local variables

Local variables for execution of method body in method call:

- Big step semantics:
only *this* and the parameters
- Small step semantics:
also access to all enclosing local variables

$$\{V:T; \text{addr } a.M([Val\ v])\} \rightarrow \{V:T; \{P:T'; P := Val\ v; e\}\}$$

if M has method body ($[P], e$)

\implies **dynamic binding** — more bug than feature

Method bodies should only access *this* and the parameters

Free variables (= global variables)

$fv :: expr \Rightarrow vname\ set$

$$fv\ (Cast\ C\ e) = fv\ e$$

$$fv\ (Val\ v) = \{\}$$

$$fv\ (e_1\ \ll bop \gg\ e_2) = fv\ e_1 \cup fv\ e_2$$

$$fv\ (Var\ V) = \{V\}$$

$$fv\ (V := e) = \{V\} \cup fv\ e$$

$$fv\ (e.F\{D\}) = fv\ e$$

$$fv\ \{V:T; e\} = fv\ e - \{V\}$$

$$fv\ (try\ e_1\ catch\ (C\ V)\ e_2) = fv\ e_1 \cup (fv\ e_2 - \{V\})$$

⋮

Weak well-formedness

Definition A program is *weakly well-formed* (*wwf-J-prog P*) iff every method body (Vs, e) uses only its own local variables, *this* and the parameters Vs :

$$fv\ e \subseteq \{this\} \cup set\ Vs$$

Equivalence

Theorem If *wwf-J-prog* P then
 $P \vdash \langle e, s \rangle \Rightarrow \langle e', s' \rangle$ iff $(P \vdash \langle e, s \rangle \rightarrow^* \langle e', s' \rangle \wedge \text{final } e')$

Proof of \Rightarrow and \Leftarrow separately.

Big \implies *small*

Theorem If *wwf-J-prog* P and $P \vdash \langle e, s \rangle \Rightarrow \langle e', s' \rangle$ then $P \vdash \langle e, s \rangle \rightarrow^* \langle e', s' \rangle$.

Proof by rule induction on \Rightarrow . Only blocks, try-catch and (especially!) method call are non-trivial.

small \implies *Big*

Theorem If *wwf-J-prog* P and $P \vdash \langle e, s \rangle \rightarrow^* \langle e', s' \rangle$ and *final* e' then $P \vdash \langle e, s \rangle \Rightarrow \langle e', s' \rangle$.

Proof by induction on \rightarrow^* .

- Basis: final expressions evaluate to themselves
- Step: by Lemma

Lemma If *wwf-J-prog* P and $P \vdash \langle e, s \rangle \rightarrow \langle e'', s'' \rangle$ and $P \vdash \langle e'', s'' \rangle \Rightarrow \langle e', s' \rangle$ then $P \vdash \langle e, s \rangle \Rightarrow \langle e', s' \rangle$.

Proof by rule induction on \rightarrow .