Concrete Semantics A Proof Assistant Approach

Tobias Nipkow

Fakultät für Informatik Technische Universität München

2014-1-26

1 Introduction

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Background
This Course

Why Semantics?

Without semantics, we do not really know what our programs mean.

We merely have a good intuition and a warm feeling.

Like the state of mathematics in the 19th century — before set theory and logic entered the scene.

Intuition is important!

- You need a good intuition to get your work done efficiently.
- To understand the average accounting program, intuition suffices.
- To write a bug-free accounting program may require more than intuition!
- I assume you have the necessary intuition.
- This course is about "beyond intuition".

Intuition is not sufficient!

Writing correct language processors (e.g. compilers, refactoring tools, ...) requires

- a deep understanding of language semantics,
- the ability to *reason* (= perform proofs) about the language and your processor.

Example:

What does the correctness of a type checker even mean? How is it proved?

Why Semantics??

We have a compiler — that is the ultimate semantics!!

- A compiler gives each individual program a semantics.
- It does not help with reasoning about the PL or individual programs.
- Because compilers are far too complicated.
- They provide the worst possible semantics.
- Moreover: compilers may differ!

The sad facts of life

- Most languages have one or more compilers.
- Most compilers have bugs.
- Few languages have a (separate, abstract) semantics.
- If they do, it will be informal (English).

Bugs

- Google "compiler bug"
- Google "hostile applet"
 Early versions of Java had various security holes.

 Some of them had to do with an incorrect bytecode verifier.

GI Dissertationspreis 2003: Gerwin Klein: *Verified Java Bytecode Verification*

Standard ML (SML)

First real language with a mathematical semantics: Milner, Tofte, Harper: The Definition of Standard ML, 1990.



Robin Milner (1934–2010) Turing Award 1991.

Main achievements:

LCF (theorem proving)
SML (functional programming)
CCS, pi (concurrency)

The sad fact of life

SML semantics hardly used:

- too difficult to read to answer simple questions quickly
- too much detail to allow reliable informal proof
- not processable beyond LaTEX, not even executable

More sad facts of life

- Real programming languages are complex.
- Even if designed by academics, not industry.
- Complex designs are error-prone.
- Informal mathematical proofs of complex designs are also error-prone.

The solution

Machine-checked language semantics and proofs

- Semantics at least type-correct
- Maybe executable
- Proofs machine-checked

The tool:

Proof Assistant (PA)
or
Interactive Theorem Prover (ITP)

Proof Assistants

- You give the structure of the proof
- The PA checks the correctness of each step
- Can prove hard and huge theorems

Government health warnings:

Time consuming
Potentially addictive
Undermines your naive trust in informal proofs

Terminology

This lecture course:

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Formal = machine-checked
Verification = formal correctness proof
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Traditionally:

Formal = mathematical

Two landmark verifications

C compiler Competitive with gcc -01



Xavier Leroy INRIA Paris using Coq

Operating system microkernel (L4)



Gerwin Klein (& Co)
NICTA Sydney
using Isabelle

A happy fact of life

Programming language researchers are increasingly using PAs

Why verification pays off

Short term: The software works!

Long term:

Tracking effects of changes by rerunning proofs

Incremental changes of the software
typically require only incremental changes of the proofs

Long term much more important than short term:

Software Never Dies

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This Course

What this course is *not* about

- Hot or trendy PLs
- Comparison of PLs or PL paradigms
- Compilers (although they will be one application)

What this course is about

- Techniques for the description and analysis of
 - PLs
 - PL tools
 - Programs
- Description techniques: operational semantics
- Proof techniques: inductions

Both informally and formally (PA!)

Our PA: Isabelle/HOL

- Developed mainly in Munich (Nipkow & Co) and Paris (Wenzel)
- Started 1986 in Cambridge (Paulson)
- The logic HOL is ordinary mathematics

Learning to use Isabelle/HOL is an integral part of the course

All exercises require the use of Isabelle/HOL

Why I am so passionate about the PA part

- It is the future
- It is the only way to deal with complex languages reliably
- I want students to learn how to write correct proofs
- I have seen too many proofs that look more like LSD trips than coherent mathematical arguments

Overview of course

- Introduction to Isabelle/HOL
- IMP (assignment and while loops) and its semantics
- A compiler for IMP
- Hoare logic for IMP
- Type systems for IMP
- Program analysis for IMP

The semantics part of the course is mostly traditional

The use of a PA is leading edge

A growing number of universities offer related course

What you learn in this course goes far beyond PLs

It has applications in compilers, security, software engineering etc.

It is a new approach to informatics