

HOMEWORK FOR LECTURE AUTOMATA AND FORMAL LANGUAGES II		
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Aufgabe 4.1. [Construction of DFTA] (10 points)
(TATA Ex. 1.8) Given the alphabet $or/2, and/2, not/1, true, false, x$. representing Boolean formula over variable x .

1. Specify a DFTA that recognizes the set of satisfiable formulas.
2. Extend the alphabet to variables $x_1, \dots, x_n$. Again, specify a DFTA that recognizes the set of satisfiable formulas.

Aufgabe 4.2. [Leaf language] (10 points)
Consider a nondeterministic word automaton $\mathcal{A} = (Q, \Sigma, I, Q_f, D)$ with states Q , alphabet Σ , initial states I , final states Q_f and rules D . Consider the tree alphabet $\mathcal{F} = f/2, x/0$ for $x \in \Sigma$. We define a function $flat : T(\mathcal{F}) \rightarrow \Sigma^*$, which returns the string of leafs, in left to right order:

$$\begin{aligned} flat(x) &= x \\ flat(f(t_1, t_2)) &= flat(t_1)flat(t_2) \end{aligned}$$

Construct an NFTA that accepts the language $L = \{t \mid flat(t) \in L(\mathcal{A})\}$. Prove your construction correct.